

fun-path-induction^{11,40}

$$\begin{aligned} & \forall T:\text{Type}, f:(T \rightarrow T), R:(T \rightarrow T \rightarrow (T \text{ List}) \rightarrow \mathbb{P}). \\ & (\forall x:T. R(x,x,[x])) \\ & \Rightarrow (\forall L:(T \text{ List}), x, y, z:T. \\ & (x = f(y)) \Rightarrow (\neg(x = y)) \Rightarrow R(y,z,[y / L]) \Rightarrow R(x,z,[x; y / L])) \\ & \Rightarrow \{\forall L:(T \text{ List}), x, y:T. x=f*(y) \text{ via } L \Rightarrow R(x,y,L)\} \end{aligned}$$